Summary: Rules on indices

$$\sqrt{\frac{16}{4}} = \sqrt{4} = 2$$

Also,
$$\sqrt{\frac{16}{4}} = \frac{\sqrt{16}}{\sqrt{4}} = \frac{4}{2} = 2$$

Both methods above are equivalent and you use whichever methods you find it easy.

So, generally,

$$\sqrt{\frac{a}{b}} = \frac{\sqrt{a}}{\sqrt{b}}$$
 or $\frac{\sqrt{a}}{\sqrt{b}} = \sqrt{\frac{a}{b}}$ use whichever method is easy.

More Facts on indces:

$$a^m \times a^n = a^{m+n}$$

$$a^m \div a^n = a^{m-n}$$

$$a^{\frac{m}{n}} = \sqrt[n]{a}^{m}$$
 or $a^{\frac{m}{n}} = \sqrt[n]{a^{m}}$

Can you see why the first method is easier even though they give the same anser

$$a^{m} = a^{mn}$$

$$a^{\frac{1}{2}} = \sqrt{a}$$

Example,

$$8^{\frac{2}{3}} = \sqrt[3]{8}^{2} = 2^{2} = 4$$
 or $8^{\frac{2}{3}} = \sqrt[3]{8^{2}} = \sqrt[3]{64} = 4$

Which of the two methods is easier and why?

Challenge: Can you show why $a^{\frac{1}{2}} = \sqrt{a}$ or $a^0 = 1$